

#### **UNIT-I**

#### INTRODUCTION

The field of robotics has its origins in science fiction. The term robot was derived from the English translation of a fantasy play written in Czechoslovakia around 1920. It took another 40 years before the modern technology of industrial robotics began. Today Robots are highly automated mechanical manipulators controlled by computers. We survey some of the science fiction stories about robots, and we trace the historical development of robotics technology. Let us begin our chapter by defining the term robotics and establishing its place in relation to other types of industrial automation.

#### **Robotics: -**

Robotics is an applied engineering science that has been referred to as a combination of machine tool technology and computer science. It includes machine design, production theory, micro electronics, computer programming & artificial intelligence.

OR

"Robotics" is defined as the science of designing and building Robots which are suitable for real life application in automated manufacturing and other non-manufacturing environments.

#### **Industrial robot: -**

The official definition of an industrial robot is provided by the robotics industries association (RIA). Industrial robot is defined as an automatic, freely programmed, servo-controlled, multi-purpose manipulator to handle various operations of an industry with variable programmed motions.

#### **Automation and robotics:-**

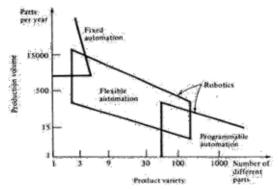
Automation and robotics are two closely related technologies. In an industrial context, we can dean automation as a technology that is concerned with the use of mechanical, electronic, and computer-based systems in the operation and control of production Examples of this technology include transfer lines. Mechanized assembly machines, feedback control systems (applied to industrial processes), numerically controlled machine tools, and robots. Accordingly, robotics is a form of industrial automation.

Ex:- Robotics, CAD/CAM, FMS, CIMS

#### **Types of Automation:-**

Automation is categorized into three types. They are,

- 1)Fixed Automation
- 2) Programmable Automation
- 3) Flexible Automation.



Relationship of fixed automation, programmable automation, and flexible automation as a tuncuon of production volume and product variety.

#### (1) Fixed Automation:-

It is the automation in which the sequence of processing or assembly operations to be carried out is fixed by the equipment configuration. In fixed automation, the sequence of operations (which are simple) are integrated in a piece of equipment. Therefore, it is difficult to automate changes in the design of the product. It is used where high volume of production is required Production rate of fixed automation is high. In this automation, no new products are processed for a given sequence of assembly operations.

#### Features:-

- i) High volume of production rates,
- ii) Relatively inflexible in product variety (no new products are produced). Ex:- Automobile industries ... etc.

#### (2) Programmable Automation:-

It is the automation in which the equipment is designed to accommodate various product configurations in order to change the sequence of operations or assembly operations by means of control program. Different types of programs can be loaded into the equipment to produce products with new configurations (i.e., new products). It is employed for batch production of low and medium volumes. For each new batch of different configured product, a new control program corresponding to the new product is loaded into the equipment. This automation is relatively economic for small batches of the product.

#### Features:-

- i) High investment in general purpose,
- ii) Lower production rates than fixed automation,
- iii) Flexibility & Changes in products configuration,
- iv) More suitable for batch production.

Ex:- Industrial robot, NC machines tools... etc.

#### (3) Flexible Automation:-

A computer integrated manufacturing system which is an extension of programmable automation is referred as flexible automation. It is developed to minimize the time loss between the changeover of the batch production from one product to another while reloading. The program to produce new products and changing the physical setup i.e., it

produces different products with no loss of time. This automation is more flexible in interconnecting work stations with material handling and storage system.

#### Features:-

- i) High investment for a custom engineering system.
- ii) Medium Production rates
- iii) Flexibility to deal with product design variation,
- iv) Continuous production of variable mixtures of products. <u>Ex:-</u> Flexible manufacturing systems (FMS)

#### Advantages:-

- 1. High Production rates
- 2. Lead time decreases
- 3. Storing capacity decreases
- 4. Human errors are eliminated.
- 5. Labour cost is decreases.

#### Disadvantages:-

- 1. Initial cost of raw material is very high,
- 2. Maintenance cost is high,
- 3. Required high skilled Labour.
- 4. Indirect cost for research development & programming increases.

#### Reasons for implementation of automated systems in manufacture industries:-

The reasons for the implementation of automated systems in manufacturing industries are as follows,

- (i) To Increase the Productivity Rate of Labour
- (ii) To Decrease the Cost of Labour
- (iii) To Minimize the Effect of Shortage of Labour
- (iv) To Obtain High Quality of Products
- (v) A Non-automation nigh Cost is Avoided
- (vi) To Decrease the Manufacturing Lead Time
- (vii) To upgrade the Safety of Workers.

#### **Need for using robotics in industries:-**

Industrial robot plays a significant role in automated manufacturing to perform different kinds of applications.

1. Robots can be built a performance capability superior to those of human beings. In terms of strength, size, speed, accuracy...etc.

- 2. Robots are better than humans to perform simple and repetitive tasks with better quality and consistence's.
- 3. Robots do not have the limitations and negative attributes of human works .such as fatigue, need for rest, and diversion of attention....etc.
- 4. Robots are used in industries to save the time compared to human beings.
- 5. Robots are in value poor working conditions
- 6. Improved working conditions and reduced risks.

#### **CAD/CAM & Robotics:-**

CAD/CAM is a term which means computer aided design and computer aided manufacturing. It is the technology concerned with the use of digital computers to perform certain functions in design & production.

<u>CAD:-</u> CAD can be defined as the use of computer systems to assist in the creation modification, analysis OR optimization of design.

<u>Cam:</u>- CAM can be defined as the use of computer system to plan, manage & control the operation of a manufacturing plant, through either direct or in direct computer interface with the plant's production resources.

#### **Specifications of robotics:-**

- 1. Axil of motion
- 2. Work stations
- 3. Speed
- 4. Acceleration
- 5. Pay load capacity
- 6. Accuracy
- 7. Repeatability etc...

#### **Overview of Robotics:-**

"Robotics" is defined as the science of designing and building Robots which are suitable for real life application in automated manufacturing and other non-manufacturing environments. It has the following objectives,

- 1. To increase productivity
- 2. Reduce production life
- 3. Minimize labour requirement
- 4. Enhanced quality of the products
- 5. Minimize loss of man hours, on account of accidents.
- 6. Make reliable and high speed production.

The robots are classified as, Programmable/Reprogrammable purpose

#### robots

- \*Tele-operated, Man controlled robots
- \*Intelligent robots.

Robots are used in manufacturing and assembly units such as,

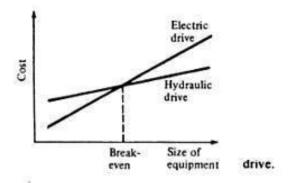
- 1. Spot or arc welding
- 2. Parts assembly
- 3. Paint spraying
- 4. Material, handling
- 5. Loading and unloading

The feature and capabilities of the robots are as follows,

- 1. Intelligence
- 2. Sensor capabilities
- 3. Telepresence
- 4. Mechanical design
- 5. Mobility and navigation
- 6. Universal gripper
- 7. System integration and networking.

## **Types of drive systems:**-

- 1. Hydraulic drive
- 2. Electric drive
- 3. Pneumatic drive



#### 1. Hydraulic drive:-

Hydraulic drive and electric drive arc the two main types of drives used on more sophisticated robots.

Hydraulic drive is generally associated with larger robots, such as the Unimate 2000 series. The usual advantages of the hydraulic drive system are that it provides the robot with greater speed and strength. The disadvantages of the hydraulic drive system are that it typically adds to the floor space required by the robot, and that a hydraulic system is inclined to leak on which is a nuisance.

This type of system can also be called as non-air powered cylinders. In this system, oil is used as a working fluid instead of compressed air. Hydraulic system need pump to generate the required pressure and flow rate. These systems are quite complex, costly and require maintenance.

#### 2. Electric drive:-

Electric drive systems do not generally provide as much speed or power as hydraulic systems. However, the accuracy and repeatability of electric drive robots are usually better. Consequently, electric robots tend to be smaller. Require less floor space, and their applications tend toward more precise work such as assembly.

In this System, power is developed by an electric current. It required little maintenance and the operation is noise less.

#### 3. Pneumatic drive:-

Pneumatic drive is generally reserved for smaller robots that possess fewer degrees of freedom (two- to four-joint motions).

In this system, air is used as a working fluid, hence it is also called air-powered cylinders. Air is compressed in the cylinder with the aid of pump the compressed air is used to generate the power with required amount of pressure and flow rates.

#### **Applications of robots:-**

#### Present Applications of Robots:-

- (i) Material transfer applications
- (ii) Machine loading and unloading
- (iii) Processing operations like,

- (a) Spot welding
- (b) Continuous arc welding
- (c) Spray coating
- (d) Drilling, routing, machining operations
- (e) Grinding, polishing debarring wire brushing
- (g) Laser drilling and cutting etc.
- (iv) Assembly tasks, assembly cell designs, parts mating.
- (v) Inspection, automation.

## Future Applications of Robots:-

The profile of the future robot based on the research activities will include the following,

- (i) Intelligence
- (ii) Sensor capabilities
- (iii) Telepresence
- (iv) Mechanical design
- (v) Mobility and navigation (walking machines)
- (vi) Universal gripper
- (vii) Systems and integration and networking
- (viii) FMS (Flexible Manufacturing Systems)
- (Ix) Hazardous and inaccessible non-manufacturing environments
- (x) Underground coal mining
- (xi) Fire fighting operations
- (xii) Robots in space
- (xiii) Security guards
- (xiv) Garbage collection and waste disposal operations
- (xv) Household robots
- (xvi) Medical care and hospital duties etc.

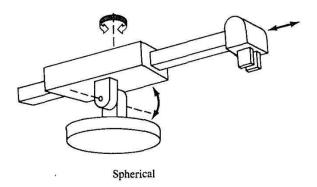
### Classification of Robots (or) Classification by co-ordinate system and control system:-

#### **Co-ordinate systems:-**

Industrial robots are available in a wide variety of sizes, shapes, and physical configurations. The vast majority of today's commercially available robots possess one of the basic configurations:

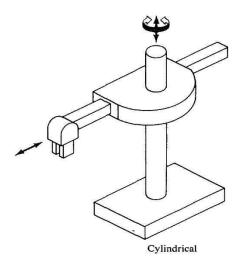
- I. Polar configuration
- 2. Cylindrical configuration
- 3. Cartesian coordinate configurable
- 4. Jointed-arm configuration

#### 1. Polar configuration:-



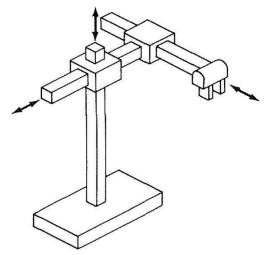
The polar configuration is pictured in part (a) of Fig. It uses a telescoping arm that can be raised or lowered about a horizontal pivot The pivot is mounted on a mta6ng base These various joints provide the robot with the capability to move its arm within a spherical space, and hence the name "spherical coordinate" robot is sometimes applied to this type. A number of commercial robots possess the polar configuration.

#### 2. Cylindrical configuration:-



The cylindrical configurable, as shown in fig, uses a vertical column and a slide that can be moved up or down along the column. The robot arm is attached to the slide so that it cm he moved radially with respect to the column. By routing the column, the robot is capable of achieving a work space that approximation a cylinder.

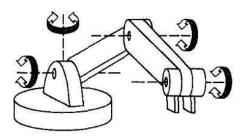
#### 3. Cartesian coordinate configurable:-



Cartesian or xyz

The cartesian coordinate robot, illustrated in part Cc) of Fig, uses three perpendicular slides to construct the x, y, and z axes. Other names are sometimes applied W this configuration, including xyz robot and rectilinear robot, By moving the three slides relative to one another, the robot is capable of operating within a rectangular work envelope.

#### 4. Jointed-arm configuration:-



Revolute

The jointed-arm robot is pictured in Fig. Its configuration is similar to that of the human arm. It consists of two straight components. Corresponding to the human forearm and upper arm, mounted on a vertical pedestal. These components are connected by two rotary joints corresponding to the shoulder and elbow.

#### **Control systems:-**

With respect to robotics, the motion control system used to control the movement of the end-effector or tool.

- 1.Limited sequence robots (Non-servo)
- 2. Playback robots with point to point (servo)
- 3. Play back robots with continuous path control,
- 4. Intelligent robots.

#### **Limited sequence robots (Non-servo):-**

Limited sequence robots do not give servo controlled to inclined relative positions of the joints; instead they are controlled by setting limit switches & are mechanical stops. There is generally no feedback associated with a limited sequence robot to indicate that the desired position, has been achieved generally thin type of robots involves simple motion as pick & place operations.

#### Point to point motion:-

These type robots are capable of controlling velocity acceleration & path of motion, from the beginning to the end of the path. It uses complex control programs, PLC's (programmable logic controller's) computers to control the motion.

The point to point control motion robots are capable of performing motion cycle that consists of a series of desired point location. The robot is tough & recorded, unit.

#### **Continuous path motion:-**

In this robots are capable of performing motion cycle in which the path followed by the robot in controlled. The robot move through a series of closely space point which describe the desired path.

Ex:- Spray painting, arc welding & complicate assembly operations.

#### **Intelligent robots:-**

This type of robots not only programmable motion cycle but also interact with its environment in a way that years intelligent. It taken make logical decisions based on sensor data receive from the operation.

There robots are usually programmed using an English like symbolic language not like a computer programming language.

#### Precision of movement (or) parameters of robot:-

The preceding discussion of response speed and stability is concerned with the dynamic performance of the robot. Another measure of performance is precision of the robot's movement. We will define precision as a function of three features:

- 1. Spatial resolution
- 2. Accuracy
- 3. Repeatability

These terms will be defined with the following assumptions.

- 1) The definitions will apply at the robot's wrist end with no hand attached to the wrist.
- 2) The terms apply to the worst case conditions, the conditions under which the robot's precision will be at its wont. This generally means that the robot's arm is fully extended in the case of a jointed arm or polar configurable.
- 3) Third, our definitions will be developed in the context of a point-to-point robot.

#### 1. Spatial resolution:-

The spatial resolution of a robot is the smallest increment of movement into which the robot can divide its work volume. Spatial resolution depends on two factors: the system's control resolution and the robot's mechanical inaccuracies. It is easiest to conceptualize these factors in terms of a robot with 1 degree of freedom.

#### 2. Accuracy:-

Accuracy refers to a robot's ability to position its wrist end at a desired target point within the work volume. The accuracy of a robot can be denned in terms of spatial resolution because the ability to achieve a given target point depends on how closely the robot can define the control increments for each of its joint motions.

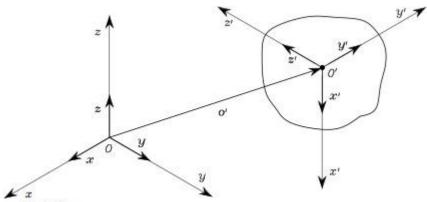
#### 3. Repeatability:-

Repeatability is concerned with the robot's ability to position its wrist or an end effector attached to its wrist at a point in space is known as repeatability. Repeatability and accuracy refer to two different aspects of the robot's precision. Accuracy relates to the robot's capacity to be programmed to achieve a given target point. The actual programmed point will probably be different from the target point due to limitations of control resolution Repeatability refers to the robot's ability to return to the programmed point when commanded to do so.

## UNIT-II KINEMATICS

Relationship between joint positions, end-effector position and orientation.

## Position of a Rigid Body



Position

$$\boldsymbol{o}' = \begin{bmatrix} o_x' \\ o_y' \\ o_z' \end{bmatrix}$$

#### Orientation

$$x' = x'_x x + x'_y y + x'_z z$$

$$y' = y'_x x + y'_y y + y'_z z$$

$$z' = z'_x x + z'_y y + z'_z z$$

## **Rotation Matrix**

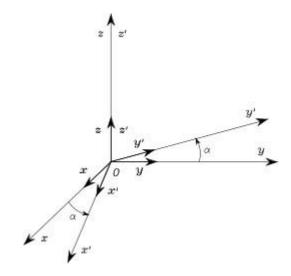
$$oldsymbol{R} = egin{bmatrix} oldsymbol{x}' & oldsymbol{y}' & oldsymbol{z}' \end{bmatrix} = egin{bmatrix} oldsymbol{x}'^Toldsymbol{x} & oldsymbol{y}'^Toldsymbol{x} & oldsymbol{z}'^Toldsymbol{x} \end{pmatrix} \ oldsymbol{z}'^Toldsymbol{z} & oldsymbol{y}'^Toldsymbol{z} & oldsymbol{z}'^Toldsymbol{z} \end{pmatrix}$$

$$\mathbf{R}^T \mathbf{R} = \mathbf{I}$$

$$\mathbf{R}^T = \mathbf{R}^{-1}$$

## **Elementary Rotation**

Rotation of α about Z



$$\boldsymbol{R}_{z}(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0\\ \sin \alpha & \cos \alpha & 0\\ 0 & 0 & 1 \end{bmatrix}$$

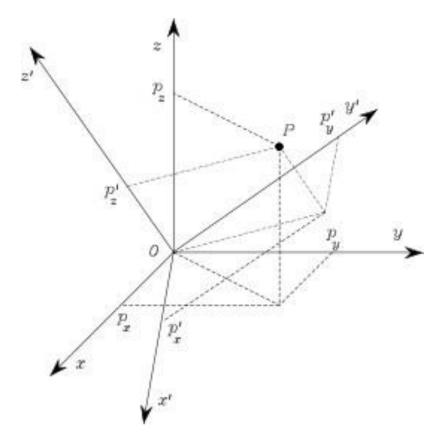
rotation of  $\beta$  about y

$$\mathbf{R}_{y}(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$$

rotation of  $\gamma$  about x

$$m{R}_x(\gamma) = egin{bmatrix} 1 & 0 & 0 \ 0 & \cos \gamma & -\sin \gamma \ 0 & \sin \gamma & \cos \gamma \end{bmatrix}$$

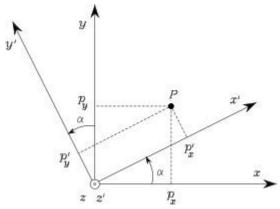
## Representation of a Vector



$$egin{aligned} oldsymbol{p} &= egin{bmatrix} p_x \ p_y \ p_z \end{bmatrix} & oldsymbol{p}' &= egin{bmatrix} p'_x \ p'_y \ p'_z \end{bmatrix} \ oldsymbol{p} &= egin{bmatrix} x' & oldsymbol{y}' & oldsymbol{z}' \end{bmatrix} oldsymbol{p}' &= oldsymbol{R} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} &= oldsymbol{R} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} &= oldsymbol{R} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} &= oldsymbol{R} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} &= oldsymbol{R} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} &= oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} &= oldsymbol{R} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} oldsymbol{P} &= oldsymbol{P} oldsymbo$$

$$\boldsymbol{p}' = \boldsymbol{R}^T \boldsymbol{p}$$

## **Example**



$$p_x = p_x' \cos \alpha - p_y' \sin \alpha$$

$$p_y = p_x' \sin \alpha + p_y' \cos \alpha$$

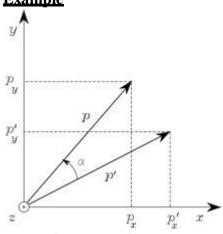
$$p_z = p'_z$$

# $\frac{\text{Rotation of a Vector}}{p = Rp'}$

$$p = Rp'$$

$$p^T p = p'^T R^T R p'$$

#### **Example**



$$p_x = p_x' \cos \alpha - p_y' \sin \alpha$$

$$p_y = p_x' \sin \alpha + p_y' \cos \alpha$$

$$p_z = p_z'$$

$$p = R_z(\alpha)p'$$

#### **Rotation matrix**

It describes the mutual orientation between two coordinate frames; its column vectors are the direction cosines of the axes of the rotated frame with respect to the original frame.

It represents the coordinate transformation between the coordinates of a point expressed in two different frames (with common origin).

It is the operator that allows the rotation of a vector in the same coordinate frame.

#### **COMPOSITION OF ROTATION MATRICES**

$$p^1 = R_2^1 p^2$$

$$oldsymbol{p}^0 = oldsymbol{R}_1^0 oldsymbol{p}^1$$

$$\boldsymbol{p}^0 = \boldsymbol{R}_2^0 \boldsymbol{p}^2$$

$$\mathbf{R}_{i}^{j} = (\mathbf{R}_{j}^{i})^{-1} = (\mathbf{R}_{j}^{i})^{T}$$

#### **Current frame rotation**

$$R_2^0 = R_1^0 R_2^1$$

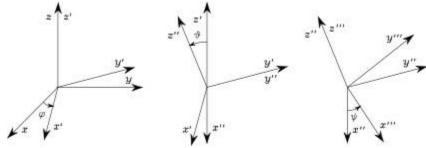
### **Fixed frame rotation**

$$R_2^0 = R_2^1 R_1^0$$

#### **EULER ANGLES**

Rotation matrix 9 parameters with 6 constraints minimal representation of orientation 3 independent parameters

## ZYZ angles



$$\begin{split} \boldsymbol{R}(\phi) &= \boldsymbol{R}_{z}(\varphi)\boldsymbol{R}_{y'}(\vartheta)\boldsymbol{R}_{z''}(\psi) \\ &= \begin{bmatrix} c_{\varphi}c_{\vartheta}c_{\psi} - s_{\varphi}s_{\psi} & -c_{\varphi}c_{\vartheta}s_{\psi} - s_{\varphi}c_{\psi} & c_{\varphi}s_{\vartheta} \\ s_{\varphi}c_{\vartheta}c_{\psi} + c_{\varphi}s_{\psi} & -s_{\varphi}c_{\vartheta}s_{\psi} + c_{\varphi}c_{\psi} & s_{\varphi}s_{\vartheta} \\ -s_{\vartheta}c_{\psi} & s_{\vartheta}s_{\psi} & c_{\vartheta} \end{bmatrix} \end{split}$$

#### **Inverse problem**

$$m{R} = egin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix}$$
 the

Given

three ZYZ angles are  $(\vartheta \in (0, \pi))$ 

$$\varphi = \text{Atan2}(r_{23}, r_{13})$$

$$\vartheta = \text{Atan2}\left(\sqrt{r_{13}^2 + r_{23}^2}, r_{33}\right)$$

$$\psi=\mathrm{Atan2}(r_{32},-r_{31})$$

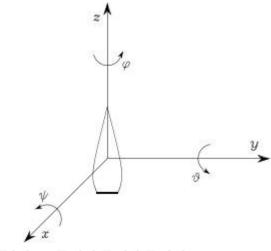
or 
$$(\vartheta \in (-\pi, 0))$$

$$\varphi = Atan2(-r_{23}, -r_{13})$$

$$\vartheta = \mathrm{Atan2}\bigg(-\sqrt{r_{13}^2 + r_{23}^2}, r_{33}\bigg)$$

$$\psi = \text{Atan2}(-r_{32}, r_{31})$$

## **RPY** angles



$$\begin{split} \boldsymbol{R}(\phi) &= \boldsymbol{R}_z(\varphi) \boldsymbol{R}_y(\vartheta) \boldsymbol{R}_x(\psi) \\ &= \begin{bmatrix} c_\varphi c_\vartheta & c_\varphi s_\vartheta s_\psi - s_\varphi c_\psi & c_\varphi s_\vartheta c_\psi + s_\varphi s_\psi \\ s_\varphi c_\vartheta & s_\varphi s_\vartheta s_\psi + c_\varphi c_\psi & s_\varphi s_\vartheta c_\psi - c_\varphi s_\psi \\ -s_\vartheta & c_\vartheta s_\psi & c_\vartheta c_\psi \end{bmatrix} \end{split}$$

## Inverse problem

$$\mathbf{R} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix}$$

Given

the three RPY angles are  $(\vartheta \in (-\pi/2, \pi/2))$ 

$$\varphi = \operatorname{Atan2}(r_{21}, r_{11})$$

$$\vartheta = \text{Atan2}\left(-r_{31}, \sqrt{r_{32}^2 + r_{33}^2}\right)$$

$$\psi = \operatorname{Atan2}(r_{32}, r_{33})$$

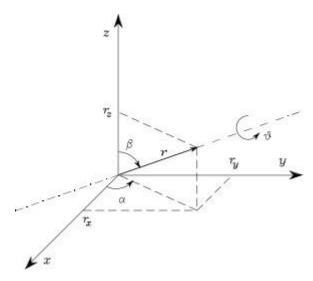
or 
$$(\vartheta \in (\pi/2, 3\pi/2))$$

$$\varphi = \operatorname{Atan2}(-r_{21}, -r_{11})$$

$$\vartheta = \text{Atan2}\left(-r_{31}, -\sqrt{r_{32}^2 + r_{33}^2}\right)$$

$$\psi = \text{Atan2}(-r_{32}, -r_{33})$$

#### **ANGLE AND AXIS**



$$R(\vartheta, r) = R_z(\alpha)R_y(\beta)R_z(\vartheta)R_y(-\beta)R_z(-\alpha)$$

$$\sin \alpha = \frac{r_y}{\sqrt{r_x^2 + r_y^2}} \qquad \cos \alpha = \frac{r_x}{\sqrt{r_x^2 + r_y^2}}$$
$$\sin \beta = \sqrt{r_x^2 + r_y^2} \qquad \cos \beta = r_z$$

$$\boldsymbol{R}(\vartheta,\boldsymbol{r}) = \begin{bmatrix} r_x^2(1-c_\vartheta) + c_\vartheta & r_x r_y(1-c_\vartheta) - r_z s_\vartheta & r_x r_z(1-c_\vartheta) + r_y s_\vartheta \\ r_x r_y(1-c_\vartheta) + r_z s_\vartheta & r_y^2(1-c_\vartheta) + c_\vartheta & r_y r_z(1-c_\vartheta) - r_x s_\vartheta \\ r_x r_z(1-c_\vartheta) - r_y s_\vartheta & r_y r_z(1-c_\vartheta) + r_x s_\vartheta & r_z^2(1-c_\vartheta) + c_\vartheta \end{bmatrix}$$

$$R(\vartheta, r) = R(-\vartheta, -r)$$

#### Inverse problem

Given

$$\boldsymbol{R} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix}$$

the angle and axis of rotation are  $(\sin 9 6= 0)$ 

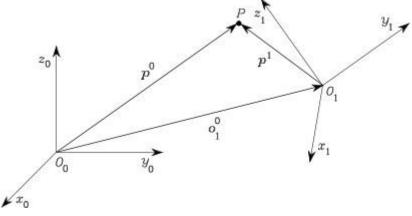
$$\vartheta = \cos^{-1}\left(\frac{r_{11} + r_{22} + r_{33} - 1}{2}\right)$$

$$\mathbf{r} = \frac{1}{2\sin\vartheta} \begin{bmatrix} r_{32} - r_{23} \\ r_{13} - r_{31} \\ r_{21} - r_{12} \end{bmatrix}$$

With

$$r_x^2 + r_y^2 + r_z^2 = 1$$

#### **HOMOGENEOUS TRANSFORMATIONS**



• Coordinate transformation (translation + rotation)

$$p^0 = o_1^0 + R_1^0 p^1$$

• Inverse transformation

$$p^1 = -R_0^1 o_1^0 + R_0^1 p^0$$

• Homogeneous representation

$$\tilde{p} = \begin{bmatrix} p \\ 1 \end{bmatrix}$$

• Homogeneous transformation matrix

$$oldsymbol{A}_1^0 = \left[ egin{array}{ccc} oldsymbol{R}_1^0 & oldsymbol{o}_1^0 \ oldsymbol{o}^T & 1 \end{array} 
ight]$$

• Coordinate transformation

$$\tilde{m{p}}^0 = m{A}_1^0 \tilde{m{p}}^1$$

• Inverse transformation

$$\tilde{oldsymbol{p}}^1 = oldsymbol{A}_0^1 ilde{oldsymbol{p}}^0 = \left(oldsymbol{A}_1^0
ight)^{-1} ilde{oldsymbol{p}}^0$$

$$oldsymbol{A}_0^1 = \left[ egin{array}{ccc} oldsymbol{R}_0^1 & & -oldsymbol{R}_0^1oldsymbol{o}_1^0 \ oldsymbol{o}^T & & 1 \end{array} 
ight]$$

$$\boldsymbol{A}^{-1} \neq \boldsymbol{A}^T$$

• Sequence of coordinate transformations

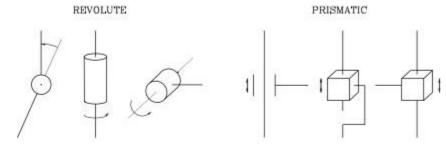
$$\tilde{\boldsymbol{p}}^0 = \boldsymbol{A}_1^0 \boldsymbol{A}_2^1 \dots \boldsymbol{A}_n^{n-1} \tilde{\boldsymbol{p}}^n$$

#### UNIT-III

## **DIRECT KINEMATICS**

#### • Manipulator

series of links connected by means of joints

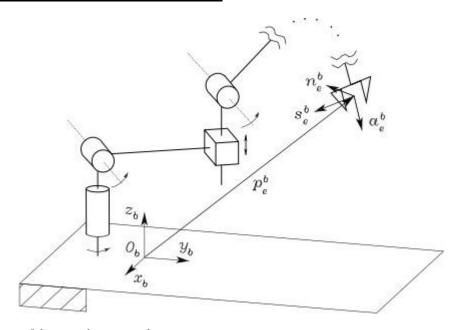


Kinematic chain (from base to end-effector) open (only one sequence) closed (loop)

## Degree of freedom

associated with a joint articulation = joint variable

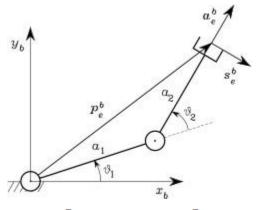
## Base frame and end-effector frame



## **Direct kinematics equation**

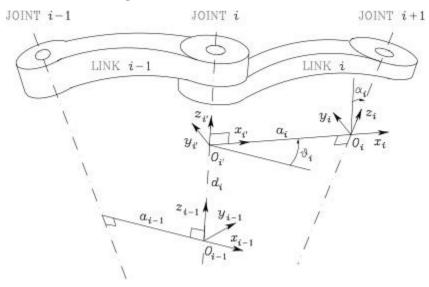
$$oldsymbol{T_e^b(oldsymbol{q}) = egin{bmatrix} oldsymbol{n_e^b(oldsymbol{q})} & oldsymbol{s_e^b(oldsymbol{q})} & oldsymbol{s_e^b(oldsymbol{q})} & oldsymbol{s_e^b(oldsymbol{q})} & oldsymbol{p_e^b(oldsymbol{q})} & oldsymbol{p_e^b(oldsymbol{q})} & oldsymbol{s_e^b(oldsymbol{q})} &$$

## Two-link planar arm



$$egin{aligned} m{T}_e^b(m{q}) &= egin{bmatrix} m{n}_e^b & m{s}_e^b & m{a}_e^b & m{p}_e^b \ 0 & 0 & 0 & 1 \end{bmatrix} \ &= egin{bmatrix} 0 & s_{12} & c_{12} & a_1c_1 + a_2c_{12} \ 0 & -c_{12} & s_{12} & a_1s_1 + a_2s_{12} \ 1 & 0 & 0 & 0 \ 0 & 0 & 0 & 1 \end{bmatrix} \end{aligned}$$

#### **Denavit-Hartenberg convention**



- choose axis z<sub>i</sub> along axis of Joint i + 1
- locate  $O_i$  at the intersection of axis  $z_i$  with the common normal to axes  $z_{i\text{-}1}$  and  $z_i$ , and  $O'_i$  at intersection of common normal with axis  $z_{i\text{-}1}$
- $\bullet$  choose axis  $x_i$  along common the normal to axes  $z_{i\text{-}1}$  and  $z_i$  with positive direction from Joint i to Joint i+1
- choose axis y<sub>i</sub> so as to complete right-handed frame
- Nonunique definition of link frame:

For Frame 0, only the direction of axis  $z_0$  is specified: then  $O_0$  and and  $X_0$  can be chosen arbitrarily.

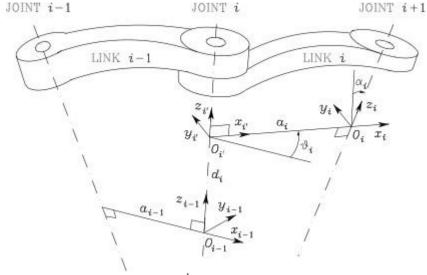
For Frame n, since there is no Joint n+1,  $z_n$  is not uniquely defined while  $x_n$  has to be normal to axis  $z_{n-1}$ ; typically Joint n is revolute and thus  $z_n$  can be aligned with  $z_{n-1}$ .

when two consecutive axes are parallel, the common normal between them is not uniquely defined.

when two consecutive axes intersect, the positive direction of  $x_i$  is arbitrary.

When Joint i is prismatic, only the direction of  $z_{i-1}$  is specified.

### **Denavit-Hartenberg parameters**



 $a_i$  distance between  $O_i$  and  $O_i$ ';

d<sub>i</sub> coordinate of O<sub>i</sub> and z<sub>i-1</sub>;

 $\alpha_i$  angle between axes z  $_{i\text{--}1}$  and z  $_i$  about axis  $x_i$  to be taken positive when rotation is made counter-clockwise

 $\upsilon_i$  angle between axes  $x_{i\text{-}1}$  and  $x_i$  about axis  $z_{i\text{-}1}$  to be taken positive when rotation is made counter-clockwise

 $a_i$  and  $\alpha_i$  are always constant

if Joint i is revolute the variable is  $v_i$ 

if Joint i is prismatic the variable is di

• Coordinate transformation

$$\boldsymbol{A}_{i'}^{i-1} = \begin{bmatrix} c_{\vartheta_i} & -s_{\vartheta_i} & 0 & 0 \\ s_{\vartheta_i} & c_{\vartheta_i} & 0 & 0 \\ 0 & 0 & 1 & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\boldsymbol{A}_{i}^{i'} = \begin{bmatrix} 1 & 0 & 0 & a_{i} \\ 0 & c_{\alpha_{i}} & -s_{\alpha_{i}} & 0 \\ 0 & s_{\alpha_{i}} & c_{\alpha_{i}} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\boldsymbol{A}_{i}^{i-1}(q_{i}) = \boldsymbol{A}_{i'}^{i-1} \boldsymbol{A}_{i}^{i'} = \begin{bmatrix} c_{\vartheta_{i}} & -s_{\vartheta_{i}} c_{\alpha_{i}} & s_{\vartheta_{i}} s_{\alpha_{i}} & a_{i} c_{\vartheta_{i}} \\ s_{\vartheta_{i}} & c_{\vartheta_{i}} c_{\alpha_{i}} & -c_{\vartheta_{i}} s_{\alpha_{i}} & a_{i} s_{\vartheta_{i}} \\ 0 & s_{\alpha_{i}} & c_{\alpha_{i}} & d_{i} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

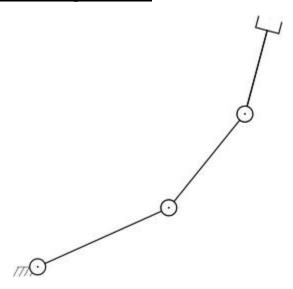
#### **Procedure**

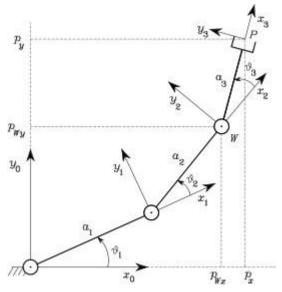
- Find and number consecutively the joint axes; set the directions of axes  $z_0, \ldots, z_{n-1}$ .
- 2. Choose Frame 0 by locating the origin on axis  $z_0$ ; axes  $x_0$  and  $y_0$  are chosen so as to obtain a righthanded frame. If feasible, it is worth choosing Frame 0 to coincide with the base frame.

Execute steps from 3 to 5 for i = 1, ..., n - 1:

- 3. Locate the origin  $O_i$  at the intersection of  $z_i$  with the common normal to axes  $z_{i-1}$  and  $z_i$ . If axes  $z_{i-1}$  and  $z_i$  are parallel and Joint i is revolute, then locate  $O_i$  so that  $d_i$ =0; if Joint i is prismatic, locate  $O_i$  at a reference position for the joint range, e.g., a mechanical limit.
- 4. Choose axis  $x_i$  along the common normal to axes  $z_{i-1}$  and  $z_i$  with direction from Joint i to Joint i+1.
- 5. Choose axis y<sub>i</sub> so as to obtain a right-handed frame to complete.
- 6. Choose Frame n; if Joint n is revolute, then align  $z_n$  with  $z_{n-1}$ , otherwise, if Joint n is prismatic, then choose  $z_n$  arbitrarily. Axis  $x_n$  is set according to step 4.
- 7. For i = 1, ..., n, form the table of parameters  $a_i, d_i, \alpha_i, \nu_i$ .
- 8. On the basis of the parameters in 7, compute the homogeneous transformation matrices  $A_i^{i-1}(q_i)$  for  $i_1, \ldots, n$ .
- 9. Compute the homogeneous transformation  $T_n^0(q)=A_1^0...A_n^{n-1}$  they yields the position and orientation of Frame n with respect to Frame 0.
- 10. Given  $T_0^b$  and  $T_e^n$ , compute the direct kinematics function as  $T_e^b(q) = T_0^b T_n^0 T_e^n$  that yields the position and orientation of the end-effector frame with respect to the base frame.

#### Three-link planar arm





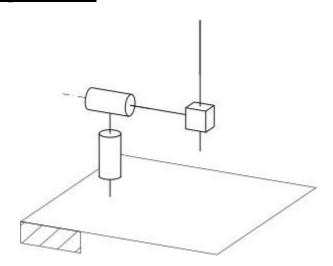
Link	$a_i$	$lpha_i$	$d_i$	$\vartheta_i$
1	$a_1$	0	0	$\vartheta_1$
2	$a_2$	0	0	$\vartheta_2$
3	$a_3$	0	0	$\vartheta_3$

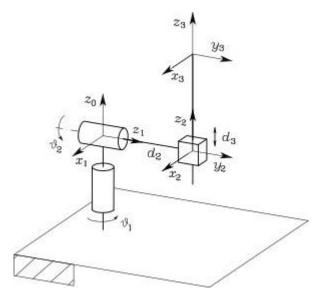
$$\boldsymbol{A}_{i}^{i-1} = \begin{bmatrix} c_{i} & -s_{i} & 0 & a_{i}c_{i} \\ s_{i} & c_{i} & 0 & a_{i}s_{i} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad i = 1, 2, 3$$

$$\boldsymbol{T}_{3}^{0} = \boldsymbol{A}_{1}^{0} \boldsymbol{A}_{2}^{1} \boldsymbol{A}_{3}^{2}$$

$$=\begin{bmatrix} c_{123} & -s_{123} & 0 & a_1c_1 + a_2c_{12} + a_3c_{123} \\ s_{123} & c_{123} & 0 & a_1s_1 + a_2s_{12} + a_3s_{123} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

## Spherical arm





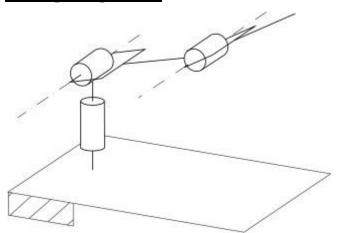
Link	$a_i$	$lpha_i$	$d_{i}$	$\vartheta_i$
1	0	$-\pi/2$	0	$\vartheta_1$
2	0	$\pi/2$	$d_2$	$\vartheta_2$
3	0	0	$d_3$	0

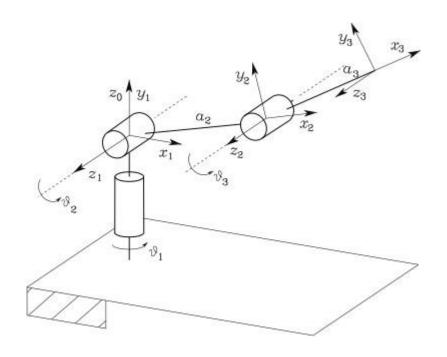
$$\boldsymbol{A}_{1}^{0} = \begin{bmatrix} c_{1} & 0 & -s_{1} & 0 \\ s_{1} & 0 & c_{1} & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \boldsymbol{A}_{2}^{1} = \begin{bmatrix} c_{2} & 0 & s_{2} & 0 \\ s_{2} & 0 & -c_{2} & 0 \\ 0 & 1 & 0 & d_{2} \\ 0 & 0 & 0 & 1 \end{bmatrix} \boldsymbol{A}_{3}^{2} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & d_{3} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\boldsymbol{T}_3^0 = \boldsymbol{A}_1^0 \boldsymbol{A}_2^1 \boldsymbol{A}_3^2$$

$$=\begin{bmatrix} c_1c_2 & -s_1 & c_1s_2 & c_1s_2d_3 - s_1d_2\\ s_1c_2 & c_1 & s_1s_2 & s_1s_2d_3 + c_1d_2\\ -s_2 & 0 & c_2 & c_2d_3\\ 0 & 0 & 0 & 1 \end{bmatrix}$$

## Anthropomorphic arm

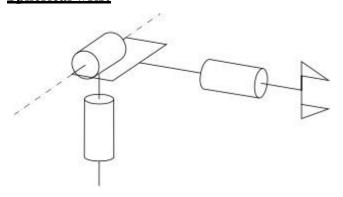


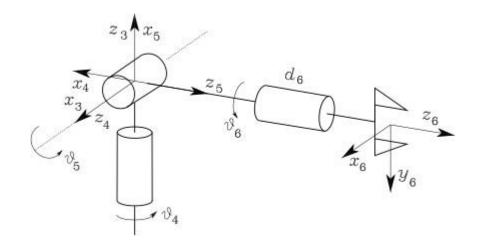


Link	$a_i$	$lpha_i$	$d_{i}$	$\vartheta_i$
1	0	$\pi/2$	0	$\vartheta_1$
2	$a_2$	0	0	$\vartheta_2$
3	$a_3$	0	0	$\vartheta_3$

$$\begin{split} \boldsymbol{A}_{1}^{0} &= \begin{bmatrix} c_{1} & 0 & s_{1} & 0 \\ s_{1} & 0 & -c_{1} & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \boldsymbol{A}_{i}^{i-1} = \begin{bmatrix} c_{i} & -s_{i} & 0 & a_{i}c_{i} \\ s_{i} & c_{i} & 0 & a_{i}s_{i} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\ \boldsymbol{T}_{3}^{0} &= \boldsymbol{A}_{1}^{0} \boldsymbol{A}_{2}^{1} \boldsymbol{A}_{3}^{2} \\ &= \begin{bmatrix} c_{1}c_{23} & -c_{1}s_{23} & s_{1} & c_{1}(a_{2}c_{2} + a_{3}c_{23}) \\ s_{1}c_{23} & -s_{1}s_{23} & -c_{1} & s_{1}(a_{2}c_{2} + a_{3}c_{23}) \\ s_{23} & c_{23} & 0 & a_{2}s_{2} + a_{3}s_{23} \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{split}$$

## **Spherical wrist**





Link	$a_i$	$lpha_i$	$d_i$	$\vartheta_i$
4	0	$-\pi/2$	0	$\vartheta_4$
5	0	$\pi/2$	0	$\vartheta_5$
6	0	0	$d_6$	$\vartheta_6$

$$\boldsymbol{A}_{4}^{3} = \begin{bmatrix} c_{4} & 0 & -s_{4} & 0 \\ s_{4} & 0 & c_{4} & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \boldsymbol{A}_{5}^{4} = \begin{bmatrix} c_{5} & 0 & s_{5} & 0 \\ s_{5} & 0 & -c_{5} & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{A}_{6}^{5} = \begin{bmatrix} c_{6} & -s_{6} & 0 & 0 \\ s_{6} & c_{6} & 0 & 0 \\ 0 & 0 & 1 & d_{6} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${\bm T}_6^3 = {\bm A}_4^3 {\bm A}_5^4 {\bm A}_6^5$$

$$=\begin{bmatrix}c_4c_5c_6-s_4s_6 & -c_4c_5s_6-s_4c_6 & c_4s_5 & c_4s_5d_6\\s_4c_5c_6+c_4s_6 & -s_4c_5s_6+c_4c_6 & s_4s_5 & s_4s_5d_6\\-s_5c_6 & s_5s_6 & c_5 & c_5d_6\\0 & 0 & 0 & 1\end{bmatrix}$$

# JOINT SPACE AND OPERATIONAL SPACE Joint space

$$oldsymbol{q} = \left[egin{array}{c} q_1 \ dots \ q_n \end{array}
ight]$$

 $q_i = \upsilon_i \; (revolute \; joint)$ 

 $q_i = d_i$  (prismatic joint)

#### **Operational space**

$$oldsymbol{x} = egin{bmatrix} oldsymbol{p} \ oldsymbol{\phi} \end{bmatrix}$$

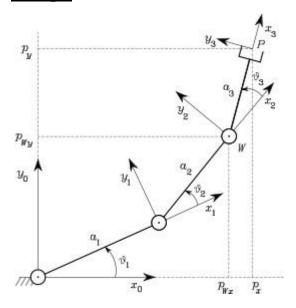
P (position)

 $\Phi$  (orientation)

## **Direct kinematics equation**

$$x = k(q)$$

## **Example**



$$\boldsymbol{x} = \begin{bmatrix} p_x \\ p_y \\ \phi \end{bmatrix} = \boldsymbol{k}(\boldsymbol{q}) = \begin{bmatrix} a_1c_1 + a_2c_{12} + a_3c_{123} \\ a_1s_1 + a_2s_{12} + a_3s_{123} \\ \vartheta_1 + \vartheta_2 + \vartheta_3 \end{bmatrix}$$

## **Workspace**

• Reachable workspace

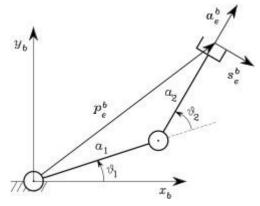
$$p = p(q) \quad q_{im} \le q_i \le q_{iM} \qquad i = 1, \ldots, n$$

surface elements of planar, spherical, toroidal and cylindrical type.

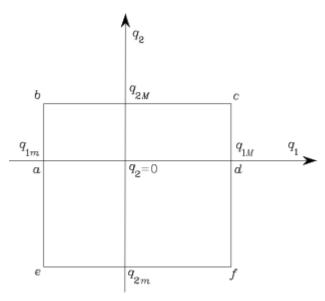
Dexterous workspace

different orientations

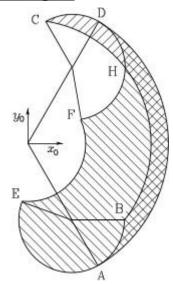
## **Example**



admissible configurations



#### **Workspace**



## **KINEMATIC CALIBRATION**

- Accurate estimates of DH parameters to improve manipulator accuracy.
- Direct kinematics equation as a function of all parameters.

$$x = k(a, \alpha, d, v)$$

x<sub>m</sub> measured pose

x<sub>n</sub> nominal pose (fixed parameters + joint variables)

$$\Delta \boldsymbol{x} = \frac{\partial \boldsymbol{k}}{\partial \boldsymbol{a}} \Delta \boldsymbol{a} + \frac{\partial \boldsymbol{k}}{\partial \boldsymbol{\alpha}} \Delta \boldsymbol{\alpha} + \frac{\partial \boldsymbol{k}}{\partial \boldsymbol{d}} \Delta \boldsymbol{d} + \frac{\partial \boldsymbol{k}}{\partial \boldsymbol{\vartheta}} \Delta \boldsymbol{\vartheta}$$

$$= \mathbf{\Phi}(\boldsymbol{\zeta}_n) \Delta \boldsymbol{\zeta}$$

1 measurements ( $lm \gg 4n$ )

$$\boldsymbol{\varDelta}\bar{\boldsymbol{x}} = \begin{bmatrix} \boldsymbol{\varDelta}\boldsymbol{x}_1 \\ \vdots \\ \boldsymbol{\varDelta}\boldsymbol{x}_l \end{bmatrix} = \begin{bmatrix} \boldsymbol{\varPhi}_1 \\ \vdots \\ \boldsymbol{\varPhi}_l \end{bmatrix} \boldsymbol{\varDelta}\boldsymbol{\zeta} = \bar{\boldsymbol{\varPhi}}\boldsymbol{\varDelta}\boldsymbol{\zeta}$$

Solution

$$\Delta \boldsymbol{\zeta} = (\bar{\boldsymbol{\Phi}}^T \bar{\boldsymbol{\Phi}})^{-1} \bar{\boldsymbol{\Phi}}^T \Delta \bar{\boldsymbol{x}}$$

$$\zeta' = \zeta_n + \Delta \zeta$$

... until  $\Delta \zeta$  converges

more accurate estimates of fixed parameters. corrections on transducers measurements.

## **INVERSE KINEMATICS PROBLEM**

• Direct kinematics

$$q \Rightarrow T$$

$$q \Rightarrow x$$

• Inverse kinematics

$$T \Rightarrow q$$

$$x \Rightarrow q$$

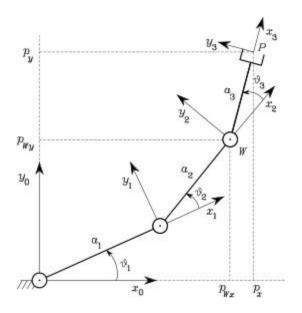
- Complexity closed-form solution multiple solutions infinite solutions no admissible solutions
- Intuition

Algebraic

Geometric

• Numerical techniques

## Solution of three-link planar arm



## Algebraic solution

$$\phi=\vartheta_1+\vartheta_2+\vartheta_3$$

$$p_{Wx} = p_x - a_3 c_\phi = a_1 c_1 + a_2 c_{12}$$

$$p_{Wy} = p_y - a_3 s_\phi = a_1 s_1 + a_2 s_{12}$$

$$c_2 = \frac{p_{Wx}^2 + p_{Wy}^2 - a_1^2 - a_2^2}{2a_1a_2}$$
 
$$s_2 = \pm \sqrt{1 - c_2^2}$$

$$\vartheta_2 = \operatorname{Atan2}(s_2, c_2)$$

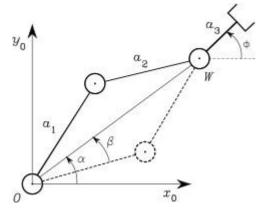
$$s_1 = \frac{(a_1 + a_2c_2)p_{Wy} - a_2s_2p_{Wx}}{p_{Wx}^2 + p_{Wy}^2}$$

$$c_1 = \frac{(a_1 + a_2 c_2)p_{Wx} + a_2 s_2 p_{Wy}}{p_{Wy}^2 + p_{Wy}^2}$$

$$\vartheta_1 = \operatorname{Atan2}(s_1, c_1)$$

$$\vartheta_3 = \phi - \vartheta_1 - \vartheta_2$$

#### Geometric solution



$$c_2 = \frac{p_{Wx}^2 + p_{Wy}^2 - a_1^2 - a_2^2}{2a_1 a_2}.$$

$$\vartheta_2 = \cos^{-1}(c_2)$$

$$\alpha = \text{Atan2}(p_{Wy}, p_{Wx})$$

$$c_{\beta} \sqrt{p_{Wx}^2 + p_{Wy}^2} = a_1 + a_2 c_2$$

$$\beta = \cos^{-1} \left( \frac{p_{Wx}^2 + p_{Wy}^2 + a_1^2 - a_2^2}{2a_1 \sqrt{p_{Wx}^2 + p_{Wy}^2}} \right)$$

$$\vartheta_1 = \alpha \pm \beta$$

# <u>UNIT-IV</u> TRAJECTORY PLANNING

• generation of reference inputs to motion control system.

Path and trajectory

Joint space trajectories

Operational space trajectories

#### PATH AND TRAJECTORY

- \* generation of suitably smooth trajectories
- Path: locus of points in joint space (operational space) which the manipulator has to follow in the execution of the assigned motion (pure geometric description)
- Trajectory: path on which a timing law is specified (e.g. velocities and/or accelerations)

#### Trajectory planning algorithm

\* inputs

path description path constraints constraints imposed by manipulator dynamics

\* outputs

joint (end-effector) trajectories in terms of time sequence of values attained by position, velocity and acceleration

- Reduced number of parameters
- \* path

extremal points
possible intermediate points geometric primitives
\* timing law

total time

max velocity and/or acceleration

velocity and/or acceleration at given points

· Operational space trajectories

- \* natural task description
- **★** path constraints
- \* singularities
- \* redundancy
- Joint space trajectories
- **★** inverse kinematics
- \* control action

#### JOINT SPACE TRAJECTORIES

- Generation of function q(t) interpolating the given vectors of joint variables at each point, in respect of the imposed constraints
  - \* the generated trajectories should be not very demanding from a computational viewpoint
  - \* the joint positions and velocities (and accelerations) should be continuous functions of time
  - \* undesirable effects should be minimized (e.g., nonsmooth trajectories)
- Point-to-point motion
  - ★ initial and final points, and traveling time
- Motion through a sequence of points
  - ★ initial and final points, intermediate points, and traveling times

Point-to-point motion

- ★ generation of q(t) describing motion from qi to qf in a time tf
- Cubic polynomial

$$q(t) = a_3 t^3 + a_2 t^2 + a_1 t + a_0$$

$$q'(t) = 3a_3t^2 + 2a_2t + a_1$$

$$q'(t) = 6a_3 t + 2a_2$$

\* computation of coefficients

$$a_0 = q_i$$

$$a_1 = \dot{q}_i$$

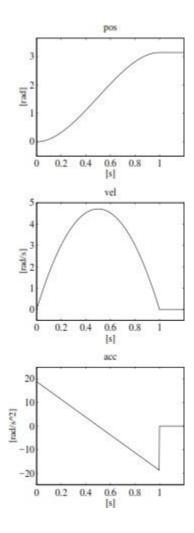
$$a_3 t_f^3 + a_2 t_f^2 + a_1 t_f + a_0 = q_f$$

$$3a_3 t_f^2 + 2a_2 t_f + a_1 = \dot{q}_f$$

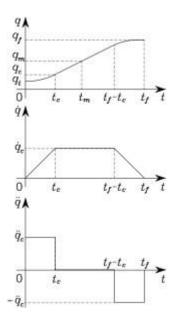
• Quintic polynomial (initial and final accelerations)

$$q(t) = a_5 t^5 + a_4 t^4 + a_3 t^3 + a_2 t^2 + a_1 t + a_0$$

Example



• Trapezoidal velocity profile



$$\ddot{q}_c t_c = \frac{q_m - q_c}{t_m - t_c}$$
 
$$q_c = q_i + \frac{1}{2} \ddot{q}_c t_c^2$$
 
$$\ddot{q}_c t_c^2 - \ddot{q}_c t_f t_c + q_f - q_i = 0$$

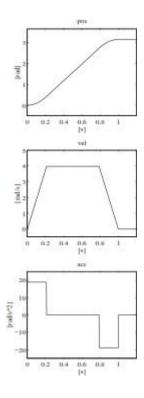
$$\ddot{q}_c$$
 specified (sgn  $\ddot{q}_c = \mathrm{sgn}\left(q_f - q_i\right)$ )

$$\begin{split} t_c &= \frac{t_f}{2} - \frac{1}{2} \sqrt{\frac{t_f^2 \ddot{q}_c - 4(q_f - q_i)}{\ddot{q}_c}} \\ |\ddot{q}_c| &\geq \frac{4|q_f - q_i|}{t_f^2} \end{split}$$

#### \* trajectory

$$q(t) = \begin{cases} q_i + \frac{1}{2}\ddot{q}_c t^2 & 0 \le t \le t_c \\ q_i + \ddot{q}_c t_c (t - t_c/2) & t_c < t \le t_f - t_c \\ q_f - \frac{1}{2}\ddot{q}_c (t_f - t)^2 & t_f - t_c < t \le t_f \end{cases}$$

## • Example



 $\dot{q}_c$  specified

$$\frac{|q_f - q_i|}{t_f} < |\dot{q}_e| \le \frac{2|q_f - q_i|}{t_f}$$
  
 $t_c = \frac{q_i - q_f + \dot{q}_c t_f}{\dot{q}_c}$ 
  
 $\ddot{q}_c = \frac{\dot{q}_c^2}{q_i - q_f + \dot{q}_c t_f}$ 

# Motion through a sequence of points

- \* opportunity to assign intermediate points (sequence of points).
- $\bullet$  For given N path points, find an interpolating function through these points N 1 order polynomial

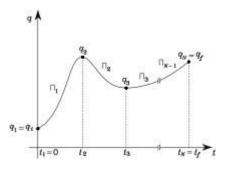
It is not possible to assign initial and final velocities as the order of polynomial increases, its oscillatory behaviour increases (not natural trajectories)

Numerical accuracy for computation of polynomial coefficients decreases as order increases

the resulting system of constraint equations is heavy to solve polynomial coefficients depend on all the assigned points

=⇒ if it is desired to change a point, all of them have to be recomputed

Sequence of low-order (cubic) interpolating polynomials continuous at path points.



- \* arbitrary values of q'(t) are imposed at path points
- \* the values of q'(t) at path points are assigned according to a certain criterion
- \* acceleration q"(t) has to be continuous at path points
- Interpolating polynomials of order less than three which determine trajectories passing nearby path points at given instants of time
- Interpolating polynomials with imposed velocities at path points.

$$\Pi_k(t_k) = q_k$$

$$\Pi_k(t_{k+1}) = q_{k+1}$$

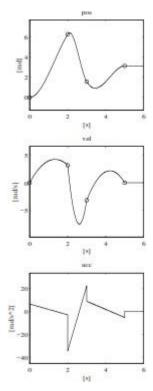
$$\dot{\Pi}_k(t_k) = \dot{q}_k$$

$$\dot{\Pi}_k(t_{k+1}) = \dot{q}_{k+1}$$

★ continuity of velocity at path points

$$\dot{\Pi}_k(t_{k+1}) = \dot{\Pi}_{k+1}(t_{k+1})$$

• Example

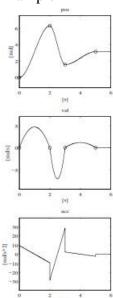


Interpolating polynomials with computed velocities at path points

$$\begin{split} \dot{q}_1 &= 0 \\ \dot{q}_k &= \begin{cases} 0 & \operatorname{sgn}\left(v_k\right) \neq \operatorname{sgn}\left(v_{k+1}\right) \\ \frac{1}{2}(v_k + v_{k+1}) & \operatorname{sgn}\left(v_k\right) = \operatorname{sgn}\left(v_{k+1}\right) \\ \dot{q}_N &= 0 \end{split}$$

$$v_k = (q_k - q_{k-1})/(t_k - t_{k-1})$$

# • Example



• Interpolating polynomials with continuous accelerations at path points (splines)

$$\begin{split} &\Pi_{k-1}(t_k) = q_k \\ &\Pi_{k-1}(t_k) = \Pi_k(t_k) \\ &\dot{\Pi}_{k-1}(t_k) = \dot{\Pi}_k(t_k) \\ &\ddot{\Pi}_{k-1}(t_k) = \ddot{\Pi}_k(t_k) \end{split}$$

- \* 4N-2 equations in 4(N-1) unknown coefficients (fourth-order polynomials for first and last segment?)
- $\star$  2 virtual points (continuity on position, velocity and acceleration) =⇒N + 1 cubic polynomials

4(N-2) equations for the N-2 intermediate path points:

$$\begin{split} & \varPi_{k-1}(t_k) = q_k \\ & \varPi_{k-1}(t_k) = \varPi_k(t_k) \\ & \dot{\varPi}_{k-1}(t_k) = \dot{\varPi}_k(t_k) \\ & \ddot{\varPi}_{k-1}(t_k) = \ddot{\varPi}_k(t_k) \end{split}$$

6 equations for the initial and final points

$$\Pi_1(t_1) = q_i$$
  
 $\dot{\Pi}_1(t_1) = \dot{q}_i$   
 $\dot{\Pi}_1(t_1) = \ddot{q}_i$   
 $\Pi_{N+1}(t_{N+2}) = q_f$   
 $\dot{\Pi}_{N+1}(t_{N+2}) = \dot{q}_f$   
 $\dot{\Pi}_{N+1}(t_{N+2}) = \ddot{q}_f$ 

6 equations for the virtual points

$$\Pi_1(t_1) = q_i$$
  
 $\tilde{\Pi}_1(t_1) = \dot{q}_i$   
 $\tilde{\Pi}_1(t_1) = \ddot{q}_i$   
 $\Pi_{N+1}(t_{N+2}) = q_f$   
 $\tilde{\Pi}_{N+1}(t_{N+2}) = \dot{q}_f$   
 $\tilde{\Pi}_{N+1}(t_{N+2}) = \ddot{q}_f$ 

\* computationally efficient algorithm

$$\ddot{\Pi}_k(t) = \frac{\ddot{\Pi}_k(t_k)}{\Delta t_k} (t_{k+1} - t) + \frac{\ddot{\Pi}_k(t_{k+1})}{\Delta t_k} (t - t_k)$$

$$\Pi_{k}(t) = \frac{\ddot{\Pi}_{k}(t_{k})}{6\Delta t_{k}} (t_{k+1} - t)^{3} + \frac{\ddot{\Pi}_{k}(t_{k+1})}{6\Delta t_{k}} (t - t_{k})^{3} + \left(\frac{\Pi_{k}(t_{k+1})}{\Delta t_{k}} - \frac{\Delta t_{k}\ddot{\Pi}_{k}(t_{k+1})}{6}\right) (t - t_{k}) + \left(\frac{\Pi_{k}(t_{k})}{\Delta t_{k}} - \frac{\Delta t_{k}\ddot{\Pi}_{k}(t_{k})}{6}\right) (t_{k+1} - t)$$

4 unknowns

N variables qk for k=2, N+1 specified continuity on q2 and qN +1 continuity on qk for  $k=3, \ldots, N$  q'i and q'f specified continuity on q'k for  $k=2, \ldots, N+1$  q'i and q'f specified

$$\dot{\Pi}_1(t_2) = \dot{\Pi}_2(t_2)$$

$$\vdots$$

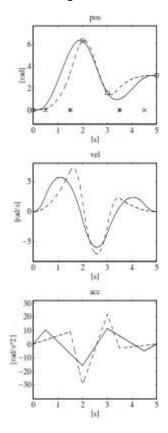
$$\dot{\Pi}_N(t_{N+1}) = \dot{\Pi}_{N+1}(t_{N+1})$$

## System of linear equations

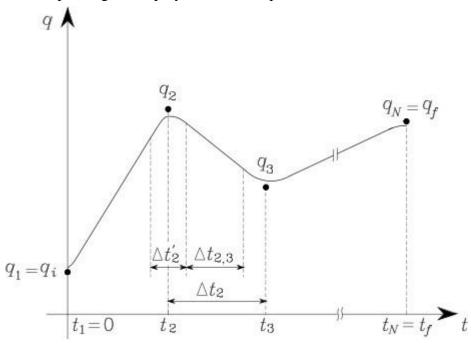
$$\mathbf{A} \begin{bmatrix} \ddot{\Pi}_2(t_2) & \dots & \ddot{\Pi}_{N+1}(t_{N+1}) \end{bmatrix}^T = \mathbf{b}$$

$$\mathbf{A} = \begin{bmatrix} a_{11} & a_{12} & \dots & 0 & 0 \\ a_{21} & a_{22} & \dots & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \dots & a_{N-1,N-1} & a_{N-1,N} \\ 0 & 0 & \dots & a_{N,N-1} & a_{NN} \end{bmatrix}$$

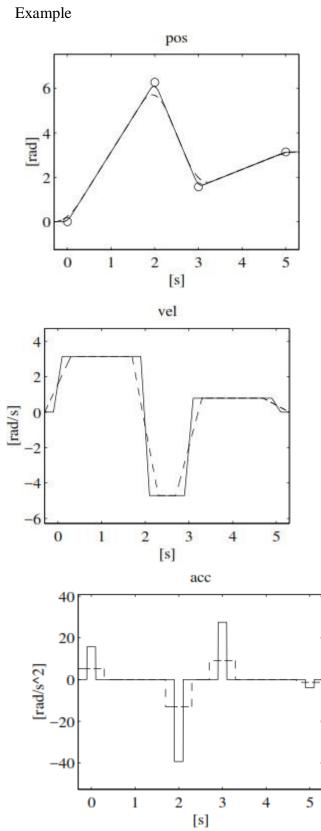
# • Example



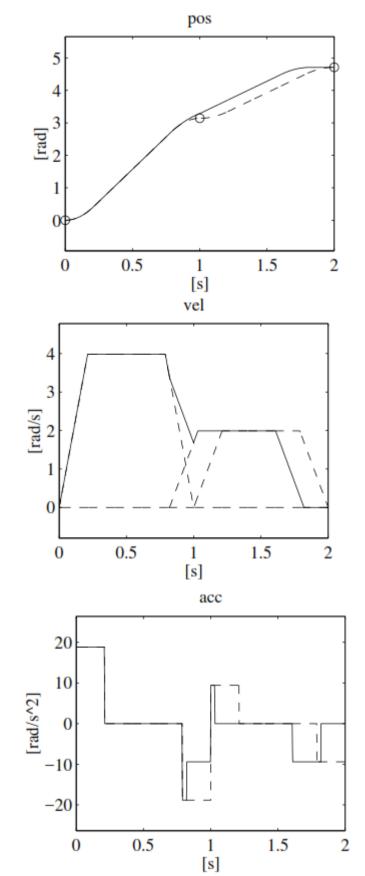
• Interpolating linear polynomials with parabolic blends



$$\dot{q}_{k-1,k} = \frac{q_k - q_{k-1}}{\Delta t_{k-1}}$$
 
$$\ddot{q}_k = \frac{\dot{q}_{k,k+1} - \dot{q}_{k-1,k}}{\Delta t_k'}$$



• Application of Trapezoidal Velocity Profile Law to Interpolation Problem



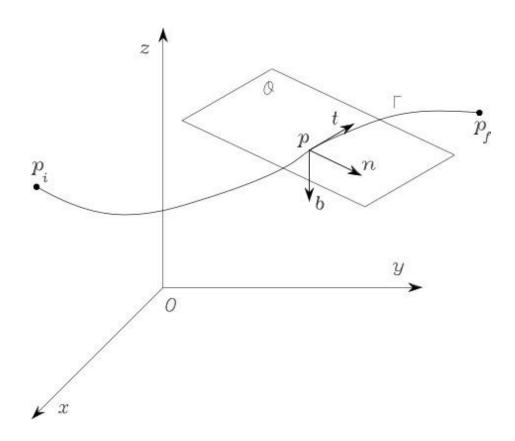
OPERATIONAL SPACE TRAJECTORIES

• Sequence of path points

- **★** inverse knematics
- ⋆ joint space trajectories
- \* microinterpolation
- Path points x(tk)
  - \* components xi(tk ) interpolated with sequence of polynomials
- Path primitives
- \* analytical description of motion

# Path primitives

• Parametric description of path in space p = f(s)

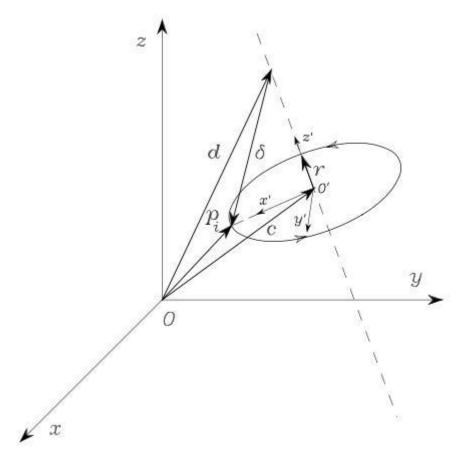


$$egin{aligned} oldsymbol{t} &= rac{doldsymbol{p}}{ds} \ oldsymbol{n} &= rac{1}{\left\| rac{d^2oldsymbol{p}}{ds^2} 
ight\|} rac{d^2oldsymbol{p}}{ds^2} \ oldsymbol{b} &= oldsymbol{t} imes oldsymbol{n} \end{aligned}$$

# Rectilinear path

$$egin{align} m{p}(s) &= m{p}_i + rac{s}{\|m{p}_f - m{p}_i\|} (m{p}_f - m{p}_i) \ & rac{dm{p}}{ds} = rac{1}{\|m{p}_f - m{p}_i\|} (m{p}_f - m{p}_i) \ & rac{d^2m{p}}{ds^2} &= m{0} \ & \end{aligned}$$

# Circular path



$$\mathbf{p}'(s) = \begin{bmatrix} 
ho \cos{(s/
ho)} \\ 
ho \sin{(s/
ho)} \\ 0 \end{bmatrix}$$

$$p(s) = c + Rp'(s)$$

$$rac{doldsymbol{p}}{ds} = oldsymbol{R} egin{bmatrix} -\sin\left(s/
ho
ight) \\ \cos\left(s/
ho
ight) \\ 0 \end{bmatrix}$$

$$\frac{d^2 \mathbf{p}}{ds^2} = \mathbf{R} \begin{bmatrix} -\cos(s/\rho)/\rho \\ -\sin(s/\rho)/\rho \\ 0 \end{bmatrix}$$

# Position and orientation trajectories

Position p =f (s)s(t) interpolating polynomial

$$\dot{\boldsymbol{p}} = \dot{s} \frac{d\boldsymbol{p}}{ds} = \dot{s} \boldsymbol{t}$$

segment

$$egin{aligned} oldsymbol{p}(s) &= oldsymbol{p}_i + rac{s}{\|oldsymbol{p}_f - oldsymbol{p}_i\|} (oldsymbol{p}_f - oldsymbol{p}_i) \ & \dot{oldsymbol{p}} &= rac{\dot{s}}{\|oldsymbol{p}_f - oldsymbol{p}_i\|} (oldsymbol{p}_f - oldsymbol{p}_i) = \dot{s}oldsymbol{t} \ & \ddot{oldsymbol{p}} &= rac{\ddot{s}}{\|oldsymbol{p}_f - oldsymbol{p}_i\|} (oldsymbol{p}_f - oldsymbol{p}_i) = \ddot{s}oldsymbol{t} \end{aligned}$$

circle

$$m{p}(s) = m{c} + m{R} egin{bmatrix} 
ho \cos{(s/
ho)} \\ 
ho \sin{(s/
ho)} \\ 0 \end{bmatrix}$$

$$\dot{\boldsymbol{p}} = \boldsymbol{R} \begin{bmatrix} -\dot{s}\sin\left(s/\rho\right) \\ \dot{s}\cos\left(s/\rho\right) \\ 0 \end{bmatrix}$$

$$\ddot{\boldsymbol{p}} = \boldsymbol{R} \begin{bmatrix} -\dot{s}^2 \cos{(s/\rho)}/\rho - \ddot{s}\sin{(s/\rho)} \\ -\dot{s}^2 \sin{(s/\rho)}/\rho + \ddot{s}\cos{(s/\rho)} \\ 0 \end{bmatrix}$$

## Orientation

interpolation of components of n(t), s(t), a(t)?

\* interpolation of P(t)

$$\phi(s) = \phi_i + \frac{s}{\|\phi_f - \phi_i\|} (\phi_f - \phi_i)$$
$$\dot{\phi} = \frac{\dot{s}}{\|\phi_f - \phi_i\|} (\phi_f - \phi_i)$$
$$\ddot{\phi} = \frac{\ddot{s}}{\|\phi_f - \phi_i\|} (\phi_f - \phi_i)$$

angle and axis (Rf = Ri Ri)

$$m{R}_f^i = m{R}_i^T m{R}_f = egin{bmatrix} r_{11} & r_{12} & r_{13} \ r_{21} & r_{22} & r_{23} \ r_{31} & r_{32} & r_{33} \end{bmatrix}$$

$$\vartheta_f = \cos^{-1}\left(\frac{r_{11} + r_{22} + r_{33} - 1}{2}\right)$$
$$r = \frac{1}{2\sin\vartheta_f} \begin{bmatrix} r_{32} - r_{23} \\ r_{13} - r_{31} \\ r_{21} - r_{12} \end{bmatrix}$$

$$m{R}^i(t)$$
:  $m{R}^i(0) = m{I}$   $m{R}^i(t_f) = m{R}^i_f$   $m{R}(t) = m{R}_i m{R}^i_r(\vartheta(t))$   $m{\vartheta}(0) = 0$   $m{\vartheta}(t_f) = m{\vartheta}_f$ 

## <u>UNIT-V</u>

# **ROBOT APPLICATION IN MANUFACTURING**

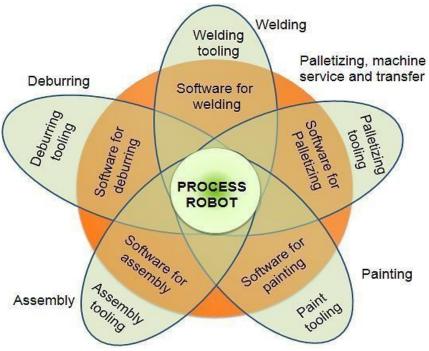


Fig. Applications of robots in industry and manufacturing

Figure shows a diagram which depicts an overview of applications of robots in manufacturing. The general characteristics of industrial work situations that tend to promote the substitution of robots for human labor.

Table Characteristics of situations where robots may substitute for humans

Situation	Description
Hazardous work environment for humans	In situations where the work environment is unsafe, unhealthy, uncomfortable, or otherwise unpleasant for humans, robot application may be considered.
Repetitive work cycle	If the sequence of elements in the work cycle is the same, and the elements consist of relatively simple motions, robots usually perform the work with greater consistency and repeatability than humans.
Difficult handling for humans	If the task requires the use of heavy or difficult-to-handle parts or tools for humans, robots may be able to perform the operation more efficiently.
Multi-shift operation	A robot can replace two or three workers at a time in second or third shifts, thus they can provide a faster financial payback.

Infrequent changeovers	Robots' use is justified for long production
	runs where there are infrequent
	changeovers, as opposed to batch or job
	shop production where changeovers are
	more frequent.
Part position and orientation are	Robots generally don't have vision
established in the work cell	capabilities, which means parts must be
	precisely placed and oriented for

# **Material Handling Applications**

Robots are mainly used in three types of applications: material handling; processing operations; and assembly and inspection. In material handling, robots move parts between various locations by means of a gripper type end effector. Material handling activity can be sub divided into material transfer and machine loading and/or unloading.

Application	Description
Material transfer	<ul> <li>Main purpose is to pick up parts at one location and place them at a new location. Part reorientation may be accomplished during the transfer. The most basic application is a pick-and-place procedure, by a low-technology robot (often pneumatic), using only up to 4 joints.</li> <li>More complex is palletizing, where robots retrieve objects from one location, and deposit them on a pallet in a specific area of the pallet, thus the deposit location is slightly different for each object transferred. The robot must be able to compute the correct deposit location via powered lead- through method, or by dimensional analysis.</li> <li>Other applications of material transfer include de-palletizing, stacking, and</li> </ul>
Machine loading and/or unloading	<ul> <li>Primary aim is to transfer parts into or out-of a production machine.</li> <li>There are three classes to consider:         <ul> <li>machine loading—where the robot loads the machine</li> <li>machine unloading—where the robot unloads the machine</li> <li>machine loading and unloading—where the robot performs both actions</li> </ul> </li> <li>Used in die casting, plastic molding, metal machining operations, forging, press-</li> </ul>

working, and heat-treating
operations.

# **Processing Operations**

In processing operations, the robot performs some processing activities such as grinding, milling, etc. on the workpart. The end effector is equipped with the specialized tool required for the respective process. The tool is moved relative to the surface of the workpart. Table outlines the examples of various processing operations that deploy robots.

Table: Robotic process operations

Process	Description
Spot Welding	Metal joining process in which two sheet
	metal parts are fused
	together at localized points of contact by
	the deployment of two
	electrodes that squeeze the metal
	together and apply an electric current.
	The electrodes constitute the spot
	welding gun, which is the end effector
	tool of the welding robot.
Arc Welding	Metal joining process that utilizes a
_	continuous rather than contact
	welding point process, in the same way as
	above. Again, the end
	effector is the electrodes used to achieve
	the welding arc. The robot must use
	continuous path control, and a jointed
	arm robot consisting of six joints is
	frequently used.
Spray Coating	Spray coating directs a spray gun at the
	object to be coated. Paint or
	some other fluid flows through the nozzle
	of the spray gun, which is
	the end effector and is dispersed and
	applied over the surface of the object.
	Again, the robot must use continuous path
	control, and is typically programmed
	using manual lead-through. Jointed arm
	robots seem to be the most common
	anatomy for this application.
Other applications	Other applications include: drilling,
	routing, and other machining
	processes; grinding, wire brushing, and
	similar operations; waterjet
	cutting; and laser cutting.

# **Work Cell Design and Control**

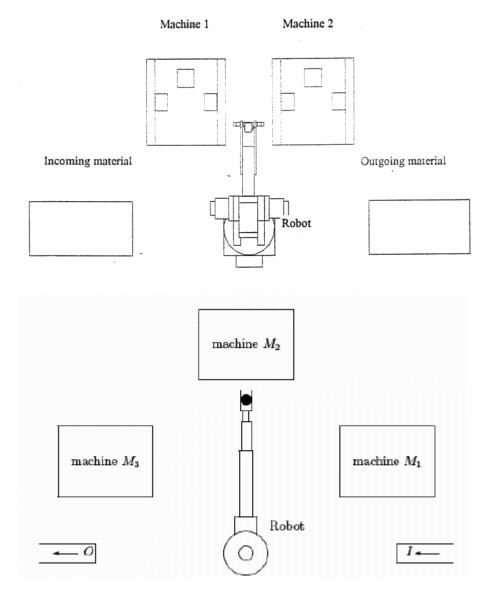
# Robot work cell layout

Robot-centered work cell

- In-line robot work cell
- Mobile work cell

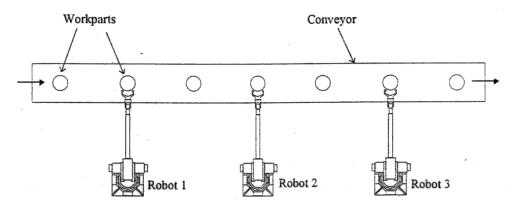
# Robot-centered work cell

- Center of work cell
- High utilization of robot
- Method of work part delivery (eg: conveyor, part-feeders, pallets)
- Install for single robot servicing 1@more production machines



# **In-line robot work cell**

- 1 @ more robots located along in-line conveyor
- Work is organized so each robot performs assembly operation on each part (eg: welding line)



There are 3 types of work part transport system used in in-line robot work cell.

- 1. Intermittent Transfer
- 2. Continuous Transfer
- 3. Non-Synchronous Transfer

#### **Intermittent Transfer**

The parts are moved in a start-and-stop motion from one station to another along the line. It is also called synchronous transfer since all parts are moved simultaneously to the next stop. The advantage of this system is that the parts are registered in a fixed location and orientation with respect to the robot during robot's work cycle.

# **Continuous Transfer**

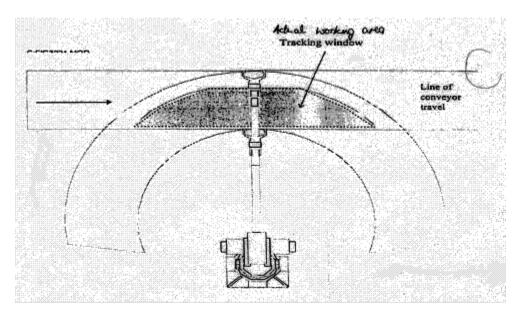
Work parts are moved continuously along the line at constant speed. The robot(s) has to perform the tasks as the parts are moving along.

The position and orientation of the parts with respect to any fixed location along the line are continuously changing.

This results in a "tracking" problem, that is, the robot must maintain the relative position and orientation of its tool with respect to the work part.

This tracking problem can be solved.

the moving baseline tracking system by moving the robot parallel to the conveyor at the same speed. or by the stationary baseline tracking system i.e. by computing and adjusting the robot tool to maintain the position and orientation with respect to the moving part.



The second tracking system involves considerable engineering problems:

- firstly, the robot must have sufficient computational and control capabilities
- secondly the robot's tracking window must be adequate
- thirdly the sensor system to identify the different parts coming into the tracking window and also to track the moving part relative to the robot's tool

## Non-synchronous Transfer System

This is a power and free system". Each work part moves independently of other parts. in a stop-and-go manner.

When a work station has finished working on a work part, that part then proceeds to the next work station. Hence, some parts are being processed on the line at the same time that others are being transported or located between stations. Here, the timing varies according to the cycle time requirements of each station.

The design and operation of this type of transfer system is more complicated than the other two because each part must be provided with its own independently operated moving cart.

However, the problem of designing and controlling the robot system used in the power-and-free method is less complicated than for the continuous transfer method.

## Nonsynchronous Transfer System

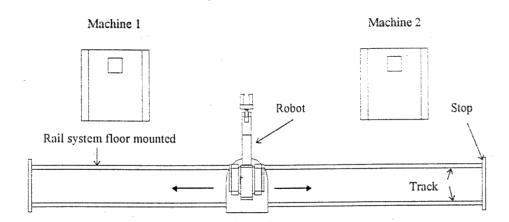
For the irregular timing of arrivals, sensors must be provided to indicate to the robot when to begin its work cycle.

The more complex problem of part registration with respect to the robot that must be solved in the continuously moving conveyor systems are not encountered on either the intermittent transfer or the non-synchronous transfer.

## Mobile work cell

In this arrangement, the robot is provided with a means of transport, such as a mobile base, within the work cell to perform various tasks at different locations.

The transport mechanism can be floor mounted tracks or overhead railing system that allows the robot to be moved along linear paths.



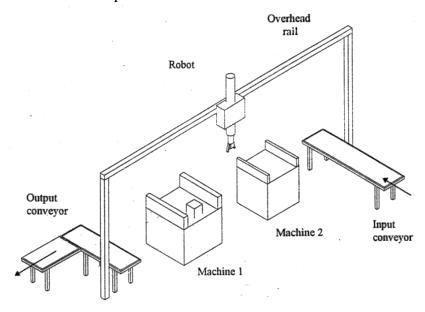
Mobile robot work cells are suitable for installations where the 1 robot must service more than one station (production machine) that has long processing cycles, and the stations cannot be arranged around the robot in a robot-centred cell arrangement.

One such reason could be due to the stations being geographically separated by distances greater than the robot's reach. The type of layout allows for time-sharing tasks that will lower the robot idle time. One of the problems in designing this work cell is to find the optimum number of stations or machines for the robot to service.

Transport mechanism: floor mounted @ overhead railing system

Service for more than one station

Problem: to find optimum number of station to service



Some Modification in Work Cell Design

Modification to other equipment in the cell Part position and orientation Part identification problem Protect of robot from its environment Utilities Control of work cell Safety

- i. Modifications to other equipment in the work cell
- Modifications need to be done in order to interface robots to equipment in the cell. Special fixtures and control devices must be devised for integrated operation.
- For example, the work holding nests. conveyor stops to position and orientate parts for robots.
- Changes has to be done in machines to allow by robots and use of limit switches and other devices to interface components

#### ii Part Position and Orientation

When parts are being delivered into the work cell, precise pick up locations along conveyors must be established.

Parts must be in a known position and orientation for the robot to grasp accurately. As the parts are being processed, the orientation must not be lost.

A way of achieving the above must be designed. For automated feeder systems, the design of the way parts are being presented to the work cell must be provided for.

## iii. Part Identification problem

It there are more than one type of parts, there will be a necessity to identify various parts by automated means, suct as optical techniques. magnetic techniques or limit switches that sense different sizes or geometry.

Electronic tagging may also be used with pallets so that the parts are identified by the information carried by the information card.

## iv. Protection of robot from its environment

In applications such as spray painting, hot metal working conditions, abrasive applications, adhesive sealant applications, the robot has to be protected from possible adverse environment. (e.g. use of sleeves, long grippers).

#### v. Utilities

Requirements for electricity. air and hydraulic pressures. gas for furnaces has to be considered and provided for.

#### vi. Control of the work cell

The activities of the robot must be coordinated with those of the other equipment in the work cell.

#### vii. Safety

Human protection measures such as fences, barriers, safety interrupt system with sensors in and around the work cell must be provided.

This must be considered even at the early stages of the design of the work cell.

Work cell control

Sequence control Operator interface Safety monitoring

Sequence control

Sequence control includes:
Regulate the sequence of activities
Control of simultaneous activities
Making decision to proceed/stop/delay work based on events

In a work cell, the sequence of activities are as follows:

- 1. Robot picks up raw work part from conveyor at a known pick up location (machine idle)
- 2. Robot loads part into fixture at machining centre (machine idle).
- 3. Machining centre begins auto machining cycle (robot idle).
- 4. Machine completes auto machining. Robot unloads machine and places part on the machine on pallet (machine idle).
- 5. Robot moves back to pick up point (machine idle)

Here almost all activities occur sequentially. Therefore, the controller must ensure activities occur in correct sequence and that each step is completed before the next is started.

Notice that machine idle / robot idle is significant. If we fit a double gripper, productivity can be further improved.

The modified sequence of activities (with double gripper fitted):

- 1. Robot picks up raw work part using the first gripper from conveyor at a known pick up location. Robot moves its double gripper into ready position in front of machining centre (machine cycle in progress).
- 2. At completion of machine cycle, robot unloads finished part from the machine fixture with a second gripper and loads raw part into fixture with the first gripper (machine idle).
- 3. Machining centre begins auto machining cycle. Robot moves finished part to pallet and places it in programmed location on pallet.
- 4. Robot moves back to pick up point (machine cycle in progress).
- In the modified sequence, several activities occur simultaneously but initiated sequentially.

Sequence Control

Therefore, controller is to ensure the various control cycles begin at the required times. a

Controller must communicate back and forth with the various equipment (machining centre. conveyors and robot).

Signals must be sent by the controller. and other signals must be received from the components. These signals are called interlocks.

## Operator Interface

Operator to interact with robot work cell.
Operator interface is required to:
Program the robot, modify and update programs
Let human operator participate in work cycle
Do data entry by human operator
Do emergency stopping activities

# **Safety Monitoring**

Emergency stopping requires an alert operator to be present to notice the emergency and take action to interrupt the cycle (however, safety emergencies do not always occur at convenient times. when the operator is present).

Therefore, a more automatic and reliable means of protecting the cell equipment and people who might wander into the work zone. is imperative. This is safety monitoring.

Safety monitoring (or hazard monitoring) is a work cell control function where sensors are used to monitor status and activities of the cell. to detect the unsafe or potentially unsafe conditions.

There are various types sensors that can be used for such purpose. for example, limit switches to detect movements has occurred correctly, temperature sensors, pressure sensitive floor mats, light beams combined with photosensitive sensors, and machine vision.

The safety monitoring is programmed to respond to various hazard conditions in different ways:

Complete stoppage of cell activities.

Slowing down the robot speed to a safe level when human is present.

Warning buzzers to alert maintenance personnel of a safety hazard.

Specially programmed subroutines to permit the robot to recover from a particular unsafe event (this is called error detection and recovery).

#### Interlock

Interlocks provide means of preventing the work cycle sequence from continuing unless a certain or set of conditions are satisfied.

This is a very important feature of work cell control, that regulates the sequence of activities being carried out. Interlocks are essential for the coordination and synchronization of activities which could not be accomplished through timing alone.

Interlocks allow for variations in the times taken for certain elements in the work cycles. In the example case in section 4. interlocks would be used for the following purposes:

To ensure that a raw part was at the pick up location. before the robot tries to grasp it.

To determine when the machining cycle has been completed before robot attempts to load part onto fixture.

To indicate that the part has been successfully loaded so that the auto machining cycle can start.

Input interlocks.

Input interlocks make use of signals sent from the components in the cell to the controller.

They indicate that certain conditions have been met and that the programmed work sequence can continue. For example a limit switch on work fixture can send a signal to indicate that the part has been properly loaded.

Output interlocks.

Makes use of signals sent from the controller to other devices or machines in the work cell.

In our example an output signal is used to signal the machining centre to commence the auto cycle. The signal is contingent upon certain conditions being met. such as, that work part has been properly loaded and the robot gripper has been moved to a safe distance. These conditions are usually determined by means of input interlocks.

In our example an output signal is used to signal the machining centre to commence the auto cycle. The signal is contingent upon certain conditions being met. such as. that work part has been properly loaded and the robot gripper has been moved to a safe distance. These conditions are usually determined by means of input interlocks.

In designing the work cell, we must not only consider the regular sequence of events during normal operation. but also the possible irregularities and malfunctions that might happen. In the regular cycle, the various sequential and simultaneous activities must be identified, together with the conditions that must be satisfied.

For the potential malfunctions, the applications engineer must determine a method of identifying that the malfunction has occurred and what action must be taken to respond to that malfunction. • Then for both the regular and the irregular events in the cycle. interlocks must be provided to accomplish the required sequence control and hazard monitoring that must occur during the work cycle.

In some cases, the interlock signals can be generated by the electronic controllers for the machines. For example NC machines would be capable of being interfaced to work cell controller to signal completion of auto machining cycle.

In other cases, the applications engineer must design the interlocks using sensors to generate the required signals.